

# Electrical Properties of Neurons

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## History of Electric Brain

- After discovery of electricity, scientists discovered that conduction from brain to muscle was mediated by flow of electricity
- In 1939, Hodgkin and Huxley discovered that axons are electrically negative at rest

## Electrical signals carried by ions

The concentration of ions within the cell is different than the concentration outside of the cell

– Some ions have higher concentration inside

- $K^+$

– Some ions have higher concentrations outside:

- $Na^+$
- $Cl^-$
- $Ca^{++}$

$A^-$		many	few
$K^+$	$K^+$	400	20
$Cl^-$	$Cl^-$	40	560
$Na^+$	$Na^+$	50	440

## Steady State - Equilibrium

- Electrical signals
  - Are departure from steady state (equilibrium)
  - Are caused by net changes in ion movement
  - Underlie information processing in neurons
- The resting membrane potential of a cell
  - Membrane potential when cell is at steady state

## Steady State - Equilibrium

- Charge balance
- No **net** movement of water
  - No change in the volume of the cell
  - No dilution of concentration gradients
- No **net** change in ion movement
  - For every  $K^+$  moving inward, there is a  $K^+$  moving outward
  - No change in concentration gradients

## Charge Balance

Charge in each compartment are approximately balanced

- Outside the cell, sum of anions = sum of cations
  - $[Na^+] + 2[Ca^{++}] + [K^+] = [Cl^-]$
- Inside the cell, sum of anions = sum of cations
  - $[Na^+] + 2[Ca^{++}] + [K^+] = [Cl^-] + [A^-]$
  - $A^-$  are other anions, which are mostly proteins
  - Anions are impermeant to the membrane

## Osmolarity Balance

- Water balance = Osmolarity balance
- Osmolarity inside cell is equal to osmolarity outside cell
- $[Na^+]_i + [Ca^{++}]_i + [K^+]_i + [Cl^-]_i + [A^-]_i = [Na^+]_o + [Ca^{++}]_o + [K^+]_o + [Cl^-]_o$
- Membrane is permeable to water. If osmolarity is different, water will flow to equalize osmolarity.

## Ion Movement

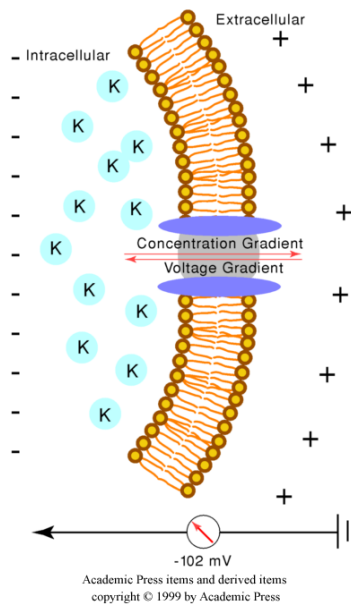
- Concentration gradient produces tendency for ions to move from high concentration to low concentration
  - Mechanism is diffusion
- Ions move through ionic channels
  - Protein pores in membrane
- At rest, pores for sodium and calcium are closed
  - Membrane is selectively permeable to potassium

## Ion Movement

- How is equilibrium maintained if  $K^+$  ions can move down concentration gradient?
- Movement of potassium from inside to outside causes slight imbalance in charge
  - Recall that anions are impermeable and can't move with potassium
  - Excess of  $K^+$  outside
  - Excess of  $A^-$  inside

## Ion Movement Forces

- Concentration gradient is balanced by voltage gradient



## Ion Movement

- Charge distribution creates an electrical field.
  - Produces a potential difference between inside and outside
- Potential difference permitted by special property of membrane
  - Capacitance
  - Farad = Coulomb per Volt
  - Quantity of charge producing a 1 volt potential.

## Ion Movement

- Potential difference produces force of attraction
  - Negative potential of cell attracts potassium ions
  - As potential decreases, the force that draws potassium ions inside the cell increases
- At some potential, electrostatic forces pulling  $K^+$  in equals diffusive tendency for  $K^+$  to move out.
  - At that potential and concentration gradient, no net flow of  $K^+$  occurs.

Resting Potential is called Equilibrium potential

## Nernst Equation

- Equilibrium potential is determined by
  - Concentration outside,  $C_{out}$
  - Concentration inside,  $C_{in}$
  - Temperature of solution in Kelvin, T
  - Valence of ion, z
  - Work required to separate charge, R

## Nernst Equation

$$E_R = \frac{RT}{zF} \ln\left(\frac{C_{out}}{C_{in}}\right)$$

- R is the ideal gas constant
  - 8.32 joules/Kelvin/mole
- F is Faraday's constant
  - 96,485 Coulombs per mole

## Squid Axon

Ion	Conc in	Conc out	Equilibrium Potential
Na <sup>+</sup>	50	440	55
K <sup>+</sup>	400	20	-76
Cl <sup>-</sup>	40	560	-66
Ca <sup>++</sup>	0.4	10	145

Concentration in millimoles,  
potential in millivolts.

## Mammalian Neuron

Ion	Conc in	Conc out	Equilibrium Potential
Na <sup>+</sup>	18	145	56
K <sup>+</sup>	135	3	-102
Cl <sup>-</sup>	7	20	-76
Ca <sup>++</sup>	0.0001	1.2	125

Concentration in millimoles,  
potential in millivolts.

Calcium is heavily buffered; thus total internal calcium is higher



## Reversal Potential

### Equilibrium potential also called reversal potential, $E_R$

- If membrane potential ( $V_M$ ) is greater than  $E_R$ , then potassium ions flow out
- If  $V_M$  is lower than  $E_R$ , then potassium ions flow in
- If  $V_M = E_R$ , then forces balance, no net flow

### In other words:

- If  $V_M - E_R > 0$ , then positive ions flow out
  - Outward current
- If  $V_M - E_R < 0$ , then positive ions flow in
  - Inward current
- If  $V_M - E_R = 0$ , no current flow

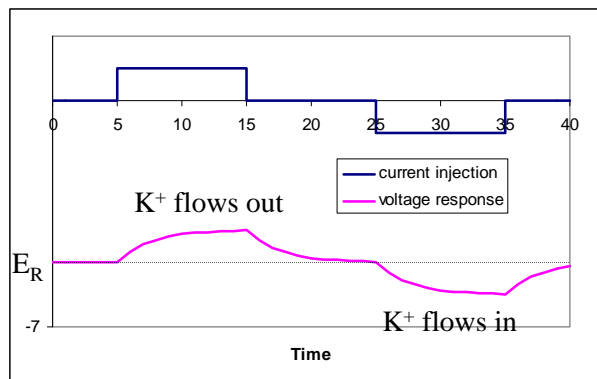
## Ion Movement controlled by $V_M$

Depolarize cell with current injection

Higher  $V_M$  implies insufficient charge to attract  $K^+$

$K^+$  moves down concentration gradient

Membrane Potential



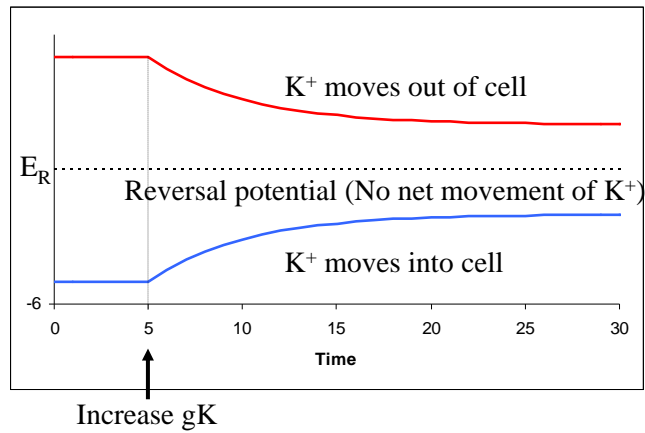
## $V_M$ controlled by Ion Movement

Tends to return membrane potential to equilibrium

1. Begin above  $E_R$

Membrane Potential

2. Begin below  $E_R$



## Resting Potential

- If membrane is permeable to  $K^+$ , then ions flow until  $V_M = E_K$
- Neuron membranes are permeable to multiple ions
  - $Cl^-$
  - $Na^+$
- Permeability is less than  $K^+$
- Permeability varies between neuronal types

## Resting Potential

- Represents a steady state
  - No net ion fluxes
  - No net water movement (osmotic balance)
  - Charge balance
- Not all neurons have steady state
  - Spontaneous activity in absence of input
  - In live brain, are any neurons in steady state?
- Varies between neuron types
  - Photoreceptors rest at -40 mV
  - Thalamic cells rest at -70 mV during sleep, -55 mV during waking
  - Spiny projection neurons alternative between -80 mV and -55 mV
  - Cortical and hippocampal neurons rest near -75 mV

## Goldman-Hodgkin-Katz Equation

- Resting potential depends on concentration of all ions to which membrane is permeable
- Relative contribution of each ion depends on
  - Concentration gradient
  - Permeability (relative to potassium)

$$V_M = \frac{RT}{F} \ln \left( \frac{p_K \cdot K_{out} + p_{Na} \cdot Na_{out} + p_{Cl} \cdot Cl_{in}}{p_K \cdot K_{in} + p_{Na} \cdot Na_{int} + p_{Cl} \cdot Cl_{out}} \right)$$

## Squid Axon

Ion	Conc in	Conc out	Equilibrium Potential
Na+	50	440	55
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Cl-	40	560	-66
Ca++	0.4	10	145

Concentration in millimoles,  
potential in millivolts.

$pK : pNa : pCl = 1.0 : 0.04 : 0.45$ ;  $T=20\text{ C}$

Calculate resting potential: ?

Based on Goldman-Hodgkin-Katz Equation:

If  $pNa = pCl = 0$ , GHK equation reduces to Nernst Equation

In squid,  $pK : pNa : pCl = 1.0 : 0.04 : 0.45$

At  $20^\circ\text{C}$ ,  $V_m = -62\text{ mV}$

In mammals,  $pCl$  is lower,  $pNa$  is lower,

Thus  $V_m$  is lower,  $-80$  to  $-90\text{ mV}$

## Concepts in Electricity

	<b>Water Flow</b>	<b>Electricity</b>	<b>Neurons</b>
<b>Driving force</b>	pressure (lb/area)	Electrical potential (Volts)	Electrical Potential (Volts)
<b>source</b>	Gravity/pump	Battery	Concentration Gradient
<b>flow</b>	Water molecules: gallons/sec	Electrons: charge/sec (Amperes)	Ions: charge/sec (Amperes)
<b>resistance</b>	narrow pipes	resistors	Membrane Channels

## Ionic Currents

- Rate of flow of ions depends on
  - Concentration gradient (Nernst Equation)
  - Membrane potential
  - Conductance of ion channels
    - Ease of ion moving through channels
    - Conductance is inverse of resistance
    - Analogous to permeability
    - Think of water moving through hose – wide hose can carry more water than narrow hose
- Current = rate of flow of electrons
  - Each ion has either
    - Extra proton (missing an electron)
    - Extra electron
  - Flow of ions creates flow of electrons
    - Rate of flow of electrons  $\propto$  rate of flow of ions
      - Exactly equal for  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Cl}^-$
      - Double for  $\text{Ca}^{2+}$

## Ionic Currents

### Relation between membrane potential, concentration gradient, conductance

- Larger conductance = larger current
- Larger difference between  $V_M$  and  $E_R$  = larger current
- If  $V_M - E_R > 0$ , Outward current
- If  $V_M - E_R < 0$ , Inward current
  
- Examples  $I = G_m (V_m - E_r)$

## Ionic Currents at Equilibrium

- $I$  is total current flowing across membrane
  - Sum of currents due to each ion is the total current
- In equilibrium, total current is zero
  - Some current positive, some currents negative

$$I_{tot} = I_{Na} + I_K + I_{Cl} =$$

$$G_{Na} (V_M - E_{Na}) + G_K (V_M - E_K) + G_{Cl} (V_M - E_{Cl})$$

## Ionic Currents at Equilibrium

- Can solve for  $V_M$  algebraically
- $V_M$  is weighted sum of reversal potentials:

$$V_M = \frac{G_{Na} E_{Na} + G_K E_K + G_{Cl} E_{Cl}}{G_{Na} + G_K + G_{Cl}}$$

- Thus,  $V_M$  can be calculated from *permeabilities* using GHK, or from *conductances* using above equation

## Active Transport

- How are concentration gradients maintained?
- Active Transport
  - Ion carriers are large proteins
  - Directly or indirectly use ATP molecules
  - Ions are moved "uphill"
  - Distinguished from channels on kinetic basis
- 40% of energy in brain used for ion carriers

## Active Transport

Classified by the following characteristics

1. Type of ions transported
2. Stoichiometry
3. Direct vs. indirect use of ATP
4. Charge transfer (depends on 1 and 2)
5. Affinity for transported ions
6. Location of pump (which membrane surface)

## Active Transport

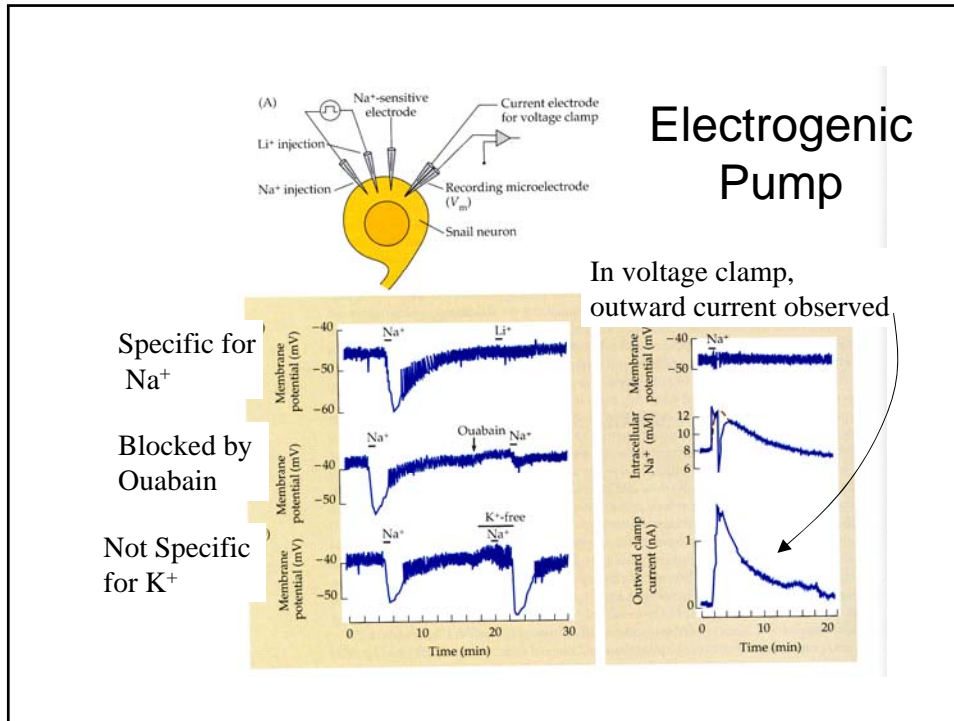
### Types of Pumps

- $\text{Na}^+$ - $\text{K}^+$  pump
- $\text{Na}^+$ - $\text{Ca}^{++}$  exchange
- $\text{Ca}^{++}$  pump
- $\text{Cl}^-$ - $\text{HCO}_3^-$  (bicarbonate) pump
- $\text{Na}^+$ - $\text{H}^+$  exchange (proton pump)
- $\text{K}^+$ - $\text{Cl}^-$  Co-transporter

## $\text{Na}^+$ - $\text{K}^+$ pump

- Stoichiometry
  - Extrudes 3  $\text{Na}^+$  for each 2  $\text{K}^+$  brought in
- Charge transfer
  - Unequal => electrogenic
  - One proton flows out for each transport cycle
  - Small current produces small hyperpolarization
- Hydrolyzes one ATP for each cycle





## Na<sup>+</sup>-K<sup>+</sup> pump Structure

### Hetero Tetramer

– Two of each of two subunits:  $\alpha$  and  $\beta$

$\alpha$ : 100 kDa

- Responsible for enzymatic activity
- 6 hydrophobic regions form transmembrane helices

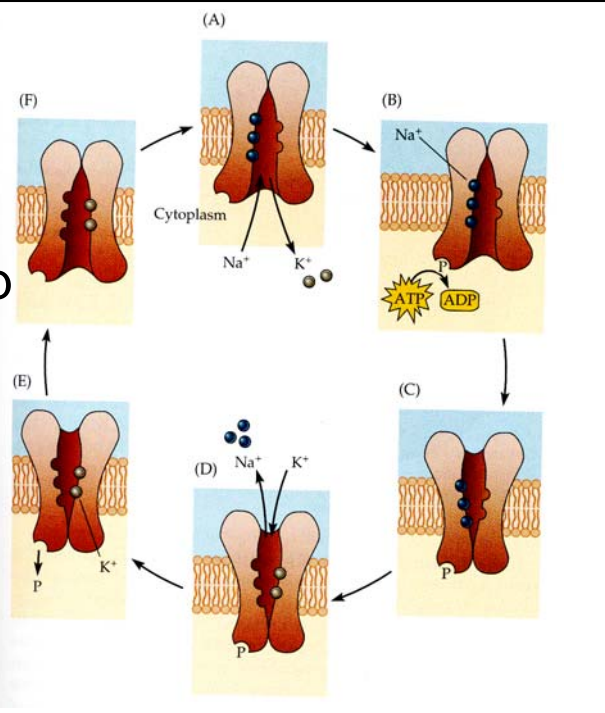
$\beta$ : 38 kDa

- 1 hydrophobic/membrane spanning segment

## Na<sup>+</sup>-K<sup>+</sup> pump Operation

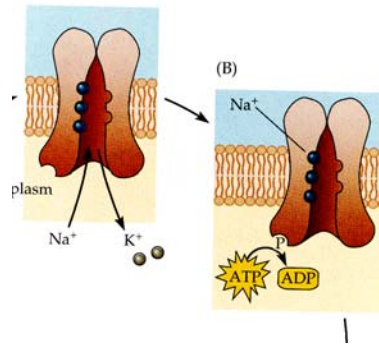
- Cation binding sites have variable specificity
  - Will only bind sodium Intracellularly
  - Will bind potassium, lithium, cesium, ammonium, rubidium extracellularly
- Sodium and potassium binding sites are exposed alternately to intracellular and extracellular solutions
  - Conformation changes driven by phosphorylation and dephosphorylation reactions

## Na<sup>+</sup>-K<sup>+</sup> Pump Operation



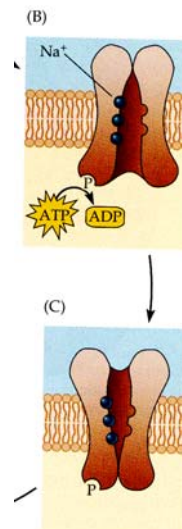
## Na<sup>+</sup>-K<sup>+</sup> Pump Operation

- A. Inward facing sites have low affinity for K<sup>+</sup> and high affinity for Na<sup>+</sup>
- B. Binding of 3 Na<sup>+</sup> causes small conformational change



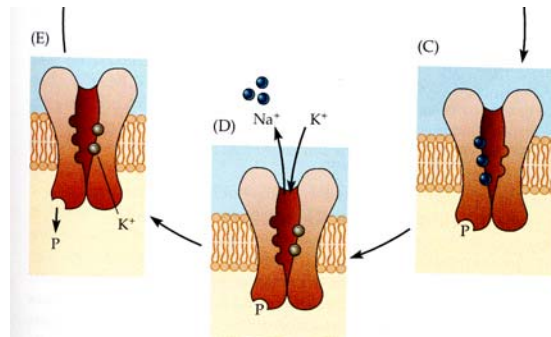
## Na<sup>+</sup>-K<sup>+</sup> Pump Operation

- C. Conformational change leads to ATP binding and phosphorylation of pump
- D. Phosphorylation produces further conformational change to expose Na<sup>+</sup> ions extracellularly



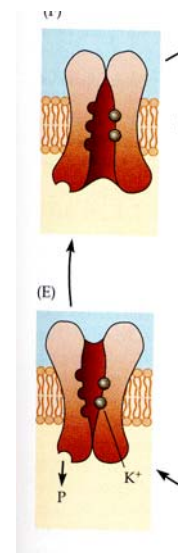
## Na<sup>+</sup>-K<sup>+</sup> Pump Operation

- E. Outward facing sites have low Na<sup>+</sup> and high K<sup>+</sup> affinities
- F. Na<sup>+</sup> ions unbind, K<sup>+</sup> ions bind



## Na<sup>+</sup>-K<sup>+</sup> Pump Operation

- G. K<sup>+</sup> binding leads to dephosphorylation
- H. Dephosphorylation leads to conformational change to expose K<sup>+</sup> Intracellularly
- I. K<sup>+</sup> leaves



## Ca<sup>2+</sup> Pumps

- Calcium is highly regulated because it influences many other processes
- Thus, there are many calcium regulatory mechanisms
  - Buffers
  - Several pumps and exchangers
  - Calcium is stored within mitochondria and ER

## Ca<sup>2+</sup> Pumps

- Calcium-magnesium ATPase pumps
  - Plasma membrane (PMCA)
    - Extrudes calcium to extracellular space
    - Binds one calcium ion each cycle
    - Affinity ~300 -600 nM
  - Smooth Endoplasmic Reticulum (SERCA)
    - Sequesters calcium in SER
    - Binds two calcium ions each cycle
    - Affinity ~100 nM

## Na<sup>+</sup>/Ca<sup>2+</sup> Exchanger (NCX)

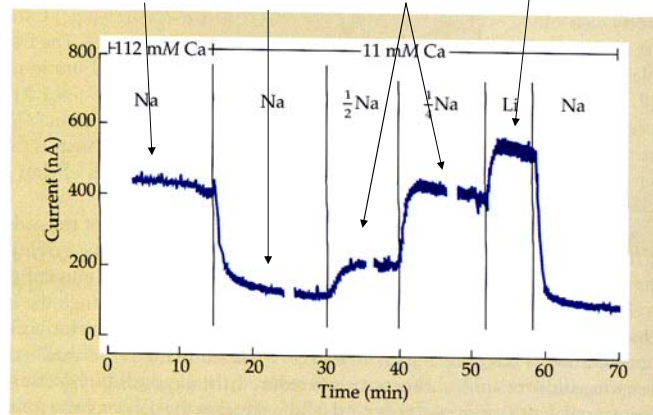
- Stoichiometry
  - 3 sodium exchanged for 1 calcium
  - Charge transfer
  - Unequal => electrogenic
  - One proton flows in for each transport cycle
  - Small current produces small depolarization

Small  
Current:  
Blocked by  
high  
Calcium

Normal  
Current

Decrease in  
current with  
reduced Na

Blocked  
by  
Lithium

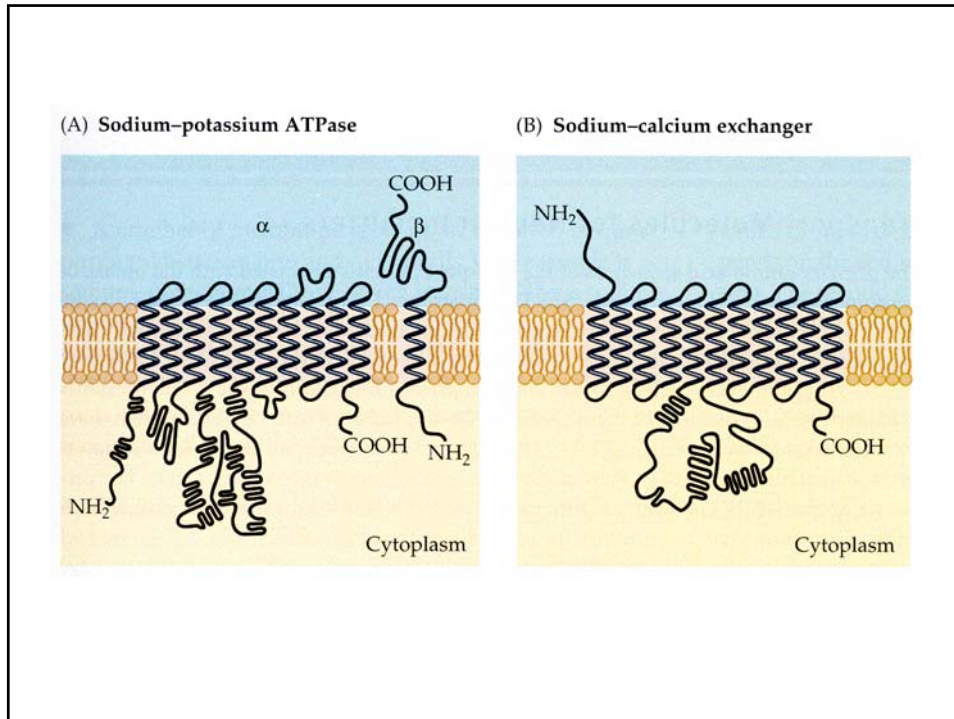


## Sodium Calcium Exchange

- Does not hydrolyze ATP
- Driven by sodium concentration gradient
  - Inward sodium removed by Na-K pump
  - *Indirectly* uses ATP
- Affinity for calcium ~ 1.0  $\mu\text{M}$
- Plasma membrane location only

## Na<sup>+</sup>/Ca<sup>2+</sup> Exchanger

- Theoretical capacity ~50x greater than PMCA
- Actual capacity depends on membrane potential
  - Depolarization may reverse pump direction
  - Reduction in concentration gradient will decrease activity and may even reverse direction
    - Increase in intracellular sodium, or
    - Decrease in extracellular sodium, or
    - Decrease in intracellular calcium, or
    - Increase in extracellular calcium
- Structure
  - 11 transmembrane segments
  - Large intracellular loop between segments 5 and 6
    - Contains regulatory domain
  - 120 kDa
  - Single subunit: 970 amino acids



## Na<sup>+</sup>/Ca<sup>2+</sup> Exchanger

- Potassium is co-factor in some neurons
  - Retinal rods
- Stoichiometry
  - 4 sodium : 1 potassium : 1 calcium
  - Additional energy from potassium gradient
- Unlikely to reverse



## Sodium Bicarbonate Exchange

- Stoichiometry
  - 1 Na<sup>+</sup> and 2 HCO<sub>3</sub><sup>-</sup> flow in, 1 Cl<sup>-</sup> pumped out
- Charge Transfer
  - Electrically neutral
- Does not hydrolyze ATP
  - Driven by Na gradient
  - Indirectly uses ATP of Na-K pump
- Regulates intracellular pH

## K<sup>+</sup>/Cl<sup>-</sup> Co-transporter (KCC)

- Several isoforms exist
  - KCC1-4
  - KCC2 is neuron specific
  - KCC4 found in peripheral neurons
- Increased expression during development causes a decrease in resting potential
- Regulated by kinases and phosphatases

## K<sup>+</sup>/Cl<sup>-</sup> Cotransporter

- Electroneutral
  - Extrudes one K<sup>+</sup> and one Cl<sup>-</sup> per cycle
- Plays a role in volume regulation
  - Activated by swelling
  - Water accompanies KCl
- Regulates chloride gradient and reversal potential

## Other Pumps

- Na<sup>+</sup>/H<sup>+</sup>
  - Electrically neutral
  - Directly passive (driven by [Na<sup>+</sup>] gradient)
  - Regulates intracellular pH
- Inward Chloride transport
  - Depends on sodium and potassium concentrations
  - Tubular cells of kidneys
  - Blocked by furosemide (lasix)

## Summary

- Resting potential = Equilibrium potential, determined by
  - Concentration gradients
    - Maintained by active transport
  - Ionic permeability
- Resting potential calculated from
  - Goldman-Hodgkin-Katz equation
  - Weighted sum of reversal potentials
- Reversal potential calculated from Nernst equation
  - Depends on concentration gradients

## Summary - Equilibrium

- A cell is in equilibrium if
  - Osmolarity is in balance (inside = outside)
  - No net flow of water (implied by above)
  - Charge is in balance (anions = cations)
  - No net flow of ions
    - Flow of ions to inside equals flow of ions to outside
- All signals considered with respect to resting potential
  - Action potentials
  - Synaptic potentials

## Summary - Electricity

- Resistance is opposite of conductance :  
 $R = 1/G$ 
  - High resistance to flow = low conductance and low permeability
- Driving force = potential difference
  - Difference between membrane potential and reversal potential:  $\Delta V = V_M - E_R$
- Each current has simple relation (Ohm's Law) to Driving force (or potential difference):
  - $I = \Delta V/R$  or  $I = \Delta V * G$